

# Performance of Genomic Prediction using Different Multi-Allelic Genomic Relationship Matrices for Genotyping-by-Sequencing (GBS) Data

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## Introduction

- Genomic prediction (GP) has been frequently implemented using GBS data since its introduction almost a decade ago.
- Genomic relationship matrices (GRM) can be derived from GBS data, and used with genomic best linear unbiased prediction (GBLUP) to perform GP.
- Short haplotypes or "short-tags", that is, multiple variants situated in small genomic segments such as those captured within GBS reads.
- Short-tags are theoretically more advantageous than single marker polymorphisms (SNP) because they are more likely to be strongly associated with causal variants. GRM-GRM constructed using short-tags are expected to be superior.

## Aim

Investigate whether predictive ability of genomic prediction can be further improved by using multi-allelic genomic relationship matrices (MA-GRM).

## Method

### MA-GRM

#### 1. Haplotype-based method (Blomhoff et al., 2014)

$$W_{HBM} = \frac{1}{n} \sum_{i=1}^n x_i x_i^T$$

where  $n$  denotes the matrix of ordered haplotype score (diagonal), and  $p$  denotes the haplotype allele frequencies.

#### 2. Haplotype similarity method (Parfitt et al., 2016)

$$W_{HSM} = \frac{1}{n} \sum_{i=1}^n x_i x_i^T$$

where  $E$  is the Kronecker product between an  $n \times n$  identity matrix

( $n =$  number of individuals) and a  $1 \times 2$  cell matrix  $\Gamma$  is the genomic relationship matrix.

#### 3. Linkage disequilibrium method (Mishra et al., 2016)

$$W_{LDM} = \frac{1}{n} \sum_{i=1}^n x_i x_i^T$$

where  $B$  is a block-diagonal matrix containing the (average) multi-allelic variance-covariance matrix of haplotypes.

### MA-GBLUP

$$y = X\beta + Z\gamma + e$$

where  $y$  is a matrix of phenotypes,  $X$  and  $Z$  are incidence matrices,  $\beta$  and  $\gamma$  are fixed and random effects with  $\text{Var}(\gamma) = G\sigma^2$  and  $e$  is the error term. In particular,  $G$  can be any

## Simulation

- 4000 GBS data of 60 ryegrass samples (with a known pedigree, Fig. 1) were simulated using *simuPOP* (Zhou et al., 2015), based on the ryegrass reference genome described in Parfitt et al. (2016).



Figure 1. Pedigree used in simulation.

- 445,100 out of 1,000,744 virtually digested GBS fragments were retained after fragment simulation at 100, 150 bp. 200,000 large simulated SNPs (2 SNPs per tag on average) with 270,000 SNPs in total.
- 1000 QTL from a quantitative trait with heritability of 0.1, 0.4, 0.7, 0.9 were simulated (1000 replicates of each scenario), with the QTL effects and residuals drawn from standard normal distributions.

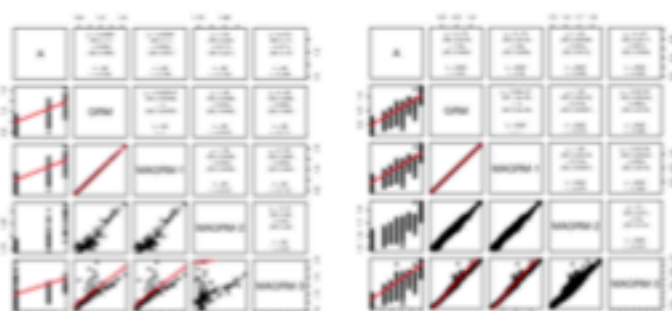


Figure 2. Pairwise correlation of diagonal (diag) and off-diagonal (off) elements within GRM.

## Results & Discussion

- The pedigree, genotype and three haplotype-based relationship matrices returned consistent results (Fig. 2), where all-diagonal and diagonal of GRMs are highly correlated (apart from the diagonal of MAHBM-G).
- Performance of GBLUP using different GRMs are almost identical (Fig. 3). However, the results may be confounded by the population size and make-up (including SNP density and linkage disequilibrium between SNPs).
- Current simulation assumed GBS data has infinite depth, the impacts of low sequencing depth and other GBS-specific sources of variation needs to be considered. Future experiments will compare the performance of methods with MA-GRM approaches in these situations.

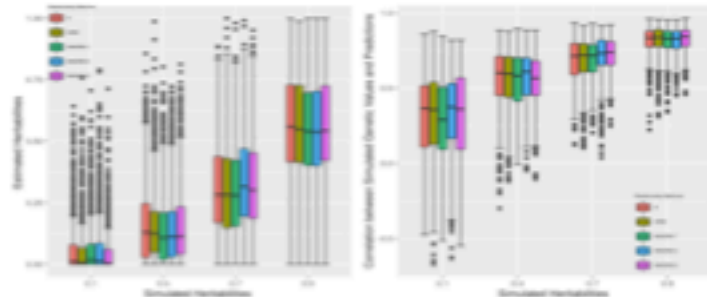


Figure 3. Performance of GBLUP using different relationship matrices. Left: correlation between diagonal and off-diagonal elements within GRM. Right: correlation between diagonal and off-diagonal elements within GRM.

## References

- Blomhoff et al. (2014). *Genetic Selection Evolution*, 45, 54.  
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## Conclusion

Despite a strong correlation between MA-GRMs and other relationship matrices, the use of MA-GRMs did not significantly improve predictive accuracy of GP under current settings.