

HSSGBLUP: a Single-Step SNP BLUP genomic evaluation software adapted to large livestock populations

Tribout T.¹, Ducrocq V.¹, Boichard D.¹

¹Université Paris-Saclay, INRAE, AgroParisTech, GABI, 78350 Jouy-en-Josas, France

Context

In France, current dairy and beef cattle genomic evaluations are based on multi-step approaches. Preselection of genotyped animals generates biased estimated breeding values and genetic trends.

Single Step GBLUP evaluations are being implemented to solve this issue, with the development of a software fitting the French bovine evaluations requirements:

- Large populations (up to 20 million animals)
- Hundreds of thousands of informative genotyped animals
- Genetic Groups
- Multiple traits evaluations, possibly with maternal genetic effects and heterogeneous variances
- Inclusion of effects of QTL or causal variants
- Inclusion of foreign phenotypic information for international populations (Holstein, BSW)
- ...

INRAE develops a software covering these features: **HSSGBLUP**. The main strategies adopted are presented here.

Current status & Perspectives

The software is completed. Optimizations (computing times) are in progress.

- All new evaluations have already been implemented with HSSGBLUP (e.g. see poster « Toward a genomic evaluation of cheese-making traits including candidate SNP in Montbeliarde cows » #110 by Sanchez et al.).
- All current French bovine polygenic and multi-step genomic evaluations will be progressively replaced by Single Step SNP BLUP evaluations before April 2022 (dairy populations) and April 2023 (beef populations).

References

- Fernando L.R., Cheng H., Golden B.L., Garrick D.J., Genet. Sel. Evol. (2016) 48:96
- Hsu W.L., Garrick D.J., Fernando R.L., G3 (Bethesda) (2017) 7(8):2685-2694
- Meuwissen T.H.E., De Jong G., Engel B., J. Dairy Sci. (1996) 79:310-316
- Taskinen M., Mantysaari E.A., Strandén I., Genet. Sel. Evol. (2017) 49:36
- Tribout T., Boichard D., Ducrocq V., Vandenplas J., 70th EAAP, Ghent (2019)
- Vandenplas J., Eding H., Calus M.P.L., 69th EAAP, Dubrovnik (2018)

The model considered is the Hybrid Single Step model proposed by Fernando et al (2016):

$$\begin{bmatrix} y_n \\ y_g \end{bmatrix} = \underbrace{\begin{bmatrix} X_n \\ X_g \end{bmatrix} \beta}_{\text{Environmental component}} + \underbrace{\begin{bmatrix} Z_n J_n \\ Z_g J_g \end{bmatrix} \mu_g}_{\text{Breeding value}} + \underbrace{\begin{bmatrix} C_n \\ 0 \end{bmatrix} \varphi}_{\text{Genetic Group component}} + \underbrace{\begin{bmatrix} Z_n & 0 \\ 0 & Z_g M_g \end{bmatrix} \begin{bmatrix} u_n \\ \alpha \end{bmatrix}}_{\text{Genetic component}} + e$$

\square_n = non genotyped animals

\square_g = genotyped animals

To ensure consistency of pedigree and genomic relationships:

μ_g = mean of unselected base animals (Hsu et al 2017)

$J_n = -A_{ng} A_{gg}^{-1} \mathbf{1}$, computed as in Tribout et al (2019)

$J_g = -\mathbf{1}$

Genetic Group component

φ = vector of genetic group effects

C_n = contributions of the Genetic Groups to non-genotyped animals

Genetic component

u_n = breeding value of non-genotyped animals

α = vector of marker effects

M_g = genotypes at markers of genotyped animals

Mixed Model Equations (example for a single trait, without maternal genetic effect)

$$\begin{bmatrix} X'X & X'_g Z_g M_g & X'_n Z_n \\ M'_g Z'_g X_g & M'_g Z'_g Z_g M_g \frac{\sigma_e^2}{\sigma_g^2} + M'_n A^{nn} M_n \frac{\sigma_e^2}{\sigma_g^2} + I \frac{\sigma_e^2}{\sigma_{\alpha_i}^2} & M'_g A^{gn} \frac{\sigma_e^2}{\sigma_g^2} \\ Z'_n X_n & A^{ng} M_g \frac{\sigma_e^2}{\sigma_g^2} & Z'_n Z_n + A^{nn} \frac{\sigma_e^2}{\sigma_g^2} \end{bmatrix} \begin{bmatrix} \hat{\beta} \\ \hat{\alpha} \\ \hat{u}_n \end{bmatrix} = \begin{bmatrix} X'y \\ M'_g Z'_g y_g \\ Z'_n y_n \end{bmatrix} * \exp(-0.5 \hat{y}_i) * \exp(-0.5 \hat{y}_i) * \exp(-0.5 \hat{y}_i)$$

$M'_g A^{nn} M_n$ computed as $M'_g A^{nn} (A^{nn})^{-1} A^{ng} M_g$ (Taskinen et al 2017), using an efficient algorithm proposed by Vandenplas et al (2018)

Inverse of pedigree relationship matrix $A^{-1} = \begin{bmatrix} A^{nn} & A^{ng} \\ A^{gn} & A^{gg} \end{bmatrix}$

M_i = (imputed) genotypes at markers of non-genotyped animals

σ_e^2 = residual variance

σ_g^2 = genetic variance

$\sigma_{\alpha_i}^2$ = genetic variance associated to the i^{th} SNP, QTL, causal variant

Inclusion of QTL or causal mutations:

$\sigma_{\alpha_i}^2$ is a function of the proportion of genetic variance explained by the i^{th} SNP, QTL, causal variant

Here, $\sigma_{\alpha_i}^2 = \exp(y_i) \sigma_e^2$ is the residual variance in the i^{th} level of heterogeneity
 \hat{y}_i are iteratively estimated on the data, as described in Meuwissen et al (1996)

The genomic relationship matrix is neither built nor inverted → the model is well adapted for populations with hundreds of thousands of genotyped animals

Programming strategies

- Coded in Fortran 90
- Solver: Preconditioned Conjugate Gradient
- Iteration on data
- Use of sparse matrices

Memory-saving strategies, making the software suitable for very large populations

- Portions of code are parallelized (openMP)
- Use of intel MKL-Pardiso library, optimized for parallelized computations on sparse matrices